

MATH 223 Fall 2023  
Assignment 8  
**Due: Friday, September 29**

**Reading**

Read carefully Sections 3.5 "Applications" in our text *Multivariable Calculus: A Linear Algebra Based Approach*.

**Writing**

Write out careful and complete solutions of Exercises 34, 36, 38, 39, 40, and 41 of Chapter 3, which also appear below.

34. Show that one parametrization of the plane  $x + 3y + 5z = 7$  is  $x = s, z = t, y = \frac{7}{3} - \frac{s}{3} - 5\frac{t}{3}$
35. (omit) Find a parametrization for the plane  $x + 3y + 5z = 7$  where  $x = s, y = t$ .
36. Find a parametrization for the plane  $x + 3y + 5z = 7$  where  $y = s, z = t$ .
37. (omit) Find a parametrization for the portion of the plane  $x + 3y + 5z = 7$  lying in the first octant (where  $x \geq 0, y \geq 0, z \geq 0$ ).
38. Show that  $x = 6 \cos s, y = 6 \sin s, z = t$  for  $0 \leq s \leq 2\pi, -1 \leq t \leq 7$  is a parametrization of the cylinder  $x^2 + y^2 = 36, -1 \leq z \leq 7$ .
39. Show that  $x = 4 \sin s \cos t, y = 4 \sin s \sin t, z = 4 \cos s$  is a parametrization of the sphere of radius 4 centered at the origin.
40. Find a parametrization of the cylinder  $x^2 + z^2 = 100$ .
41. Find a parametrization of the cylinder  $y^2 + z^2 = 100$ .