

MATH 223 Fall 2023  
Assignment 4  
**Due: Wednesday September 20**

**Reading**

Read carefully Sections 3.1 “Some Examples” and Section 3.2 “Graphs and Level Sets” in our text *Multivariable Calculus: A Linear Algebra Based Approach*.

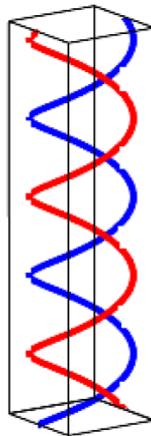
*Optional Reading:* Section 2.6.2: “Kepler’s Laws of Planetary Motion”

**Writing**

Write out careful and complete solutions of Exercises 35, 40, 42, 43 in Chapter 2 and Problem A below:

Problem A: Let  $\mathbf{f}(t) = (a \cos t, a \sin t, bt)$  with  $a$  and  $b$  nonzero constants. Sketch the graph of this curve (a **helix**) for  $0 \leq t \leq 5\pi$ . Show that the speed is constant and the velocity vector is always orthogonal to the vector  $\mathbf{r}(t) = (a \cos t, a \sin t, 0)$ .

The choices  $a = 1, b = \frac{1}{2}$  and  $a = -1, b = \frac{1}{2}$  give the general configuration of the double helix portion of the DNA molecule shown here:



*Some Answers and Hints*

**40.** Are any of these vectors orthogonal to other vectors? Point in the same direction as other vectors?

**42.** Integration by parts on  $t e^t$ , change of variable  $u = 1 + t^2$  on third component. Among the constants of integration may be 1, 0, and  $-2/3$ .

**43.** To find  $\int \tan t \, dt$ , begin by writing tangent as sine/cosine. To find  $\int \ln t \, dt$ , integration by parts may be useful.

**A.** Speed is  $\sqrt{a^2 + b^2}$ . One way to show orthogonality is to show dot product is 0.