

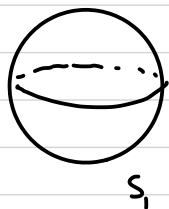
(recall: defn  $h: \mathbb{R}^2 \rightarrow \mathbb{R}^2$  diffeomorphism)

Defn  $f: S_1 \rightarrow S_2$  is a diffeomorphism if it is

- $f$  is 1-1 and onto
- $f$  is diffble
- $f^{-1}$  is diffble.  $\rightsquigarrow$  if such  $f$  exist, say  $S_1$  and  $S_2$  are diffeomorphic

Idea: Diffeomorphic surfaces are the same from the point of view of differential topology.  $S_1$  can be smoothly deformed into  $S_2$  w/o cuts or poking holes.

Ex: sphere/ellipsoid are diffeomorphic.



Ex  $f: \text{cylinder} \rightarrow \text{sphere}$  above not a diffeomorphism.